

7. Mensuration

1 mark Questions

- The curved surface area of a right circular cone of height 15 cm and base diameter 16 cm is
(A) $60\pi\text{ cm}^2$ (B) $68\pi\text{ cm}^2$ (C) $120\pi\text{ cm}^2$ (D) $136\pi\text{ cm}^2$
- If two solid hemispheres of same base radius r units are joined together along their bases, then curved surface area of this new solid is MAY-22
(A) $4\pi r^2$ sq. units (B) $6\pi r^2$ sq. units (C) $3\pi r^2$ sq. units (D) $8\pi r^2$ sq. units
- The height of a right circular cone whose radius is 5 cm and slant height is 13 cm will be SEP-21
(A) 12 cm (B) 10 cm (C) 13 cm (D) 5 cm
- If the radius of the base of a right circular cylinder is halved keeping the same height, then the ratio of the volume of the cylinder thus obtained to the volume of original cylinder is JUL-22
(A) $1 : 2$ (B) $1 : 4$ (C) $1 : 6$ (D) $1 : 8$
- The total surface area of a cylinder whose radius is $\frac{1}{3}$ of its height is PTA-1
(A) $\frac{9\pi h^2}{8}$ sq. units (B) $24\pi h^2$ sq. units (C) $\frac{8\pi h^2}{9}$ sq. units (D) $\frac{56\pi h^2}{9}$ sq. units
- In a hollow cylinder, the sum of the external and internal radii is 14 cm and the width is 4 cm . If its height is 20 cm , the volume of the material in it is PTA-4
(A) $5600\pi\text{ cm}^3$ (B) $1120\pi\text{ cm}^3$ (C) $56\pi\text{ cm}^3$ (D) $3600\pi\text{ cm}^3$
- If the radius of the base of a cone is tripled and the height is doubled then the volume is
(A) made 6 times (B) **made 18 times** (C) made 12 times (D) unchanged
- The total surface area of a hemi-sphere is how much times the square of its radius. PTA-3, SEP-21, JUL-22
(A) π (B) 4π (C) 3π (D) 2π
- A solid sphere of radius $x\text{ cm}$ is melted and cast into a shape of a solid cone of same radius. The height of the cone is
(A) $3x\text{ cm}$ (B) $x\text{ cm}$ (C) **$4x\text{ cm}$** (D) $2x\text{ cm}$
- A frustum of a right circular cone is of height 16 cm with radii of its ends as 8 cm and 20 cm . Then, the volume of the frustum is
(A) **$3328\pi\text{ cm}^3$** (B) $3228\pi\text{ cm}^3$ (C) $3240\pi\text{ cm}^3$ (D) $3340\pi\text{ cm}^3$
- A shuttle cock used for playing badminton has the shape of the combination of
(A) a cylinder and a sphere (B) a hemisphere and a cone
(C) a sphere and a cone (D) **frustum of a cone and a hemisphere**
- A spherical ball of radius r_1 units is melted to make 8 new identical balls each of radius r_2 units. Then $r_1 : r_2$ is PTA-6, SEP-20
(A) **2 : 1** (B) 1 : 2 (C) 4 : 1 (D) 1 : 4

13. The volume (in cm³) of the greatest sphere that can be cut off from a cylindrical log of wood of base radius 1 cm and height 5 cm is
 (A) $\frac{4}{3}\pi$ (B) $\frac{10}{3}\pi$ (C) 5π (D) $\frac{20}{3}\pi$
14. The height and radius of the cone of which the frustum is a part are h_1 units and r_1 units respectively. Height of the frustum is h_2 units and radius of the smaller base is r_2 units. If $h_2:h_1 = 1:2$ then $r_2:r_1$ is
 (A) 1:3 (B) 1:2 (C) 2:1 (D) 3:1 PTA-2
15. The ratio of the volumes of a cylinder, a cone and a sphere, if each has the same diameter and same height is
 (A) 1:2:3 (B) 2:1:3 (C) 1:3:2 (D) 3:1:2 PTA-5

2 mark Questions

1. The radius and height of a cylinder in the ratio 5:7 and its curved surface area is 5500sq. cm Find its radius and height. JUL-22

$$\frac{\text{Radius}}{\text{Height}} = \frac{r}{h} = \frac{5}{7} \Rightarrow r = \frac{5h}{7} \dots\dots\dots(1)$$

CSA of the cylinder = $2\pi rh = 5500$

$$2 \times \frac{22}{7} \times \frac{5h}{7} \times h = 5500$$

$$h^2 = \frac{5500 \times 7 \times 7}{2 \times 22 \times 5}$$

$$= 5 \times 5 \times 7 \times 7$$

$$h = 35\text{cm}$$

Substitute $h=35$ in (1), $r = \frac{5(35)}{7} \Rightarrow r = 25\text{cm}$.

$r = 25 \text{ cm, } h = 35\text{cm}$

2. The ratio of the radii of two right circular cones of same height is 1:3. Find the ratio of their curved surface area when the height of each cone is 3 times the radius of the smaller cone.

Smaller cone:

$$r_1 \rightarrow r$$

$$h_1 \rightarrow 3r$$

$$l_1 = \sqrt{(3r)^2 + r^2} = \sqrt{10r^2} = r\sqrt{10}$$

CSA of small cone : CSA of large cone

$$\pi r_1 l_1 : \pi r_2 l_2$$

$$r \times r\sqrt{10} : 3r \times 3r\sqrt{2}$$

$$\sqrt{5} \sqrt{2} : 9\sqrt{2}$$

$$\sqrt{5} : 9$$

Ratio of the CSA is $\sqrt{5} : 9$

Large cone:

$$r_2 \rightarrow 3r$$

$$h_2 \rightarrow 3r$$

$$l_2 = \sqrt{(3r)^2 + (3r)^2} = \sqrt{18r^2} = \sqrt{9 \times 2}(r) = 3r\sqrt{2}$$

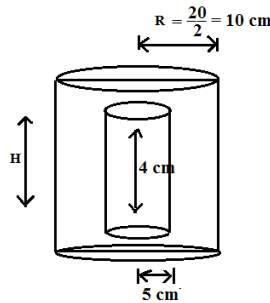
PTA-2

3. A cylindrical glass with diameter 20 cm has water to a height of 9 cm. A small cylindrical metal of radius 5 cm and height 4 cm is immersed it completely. Calculate the raise of the water in the glass?

SEP-20

Volume of water raised in cylindrical glass
= Volume of cylindrical metal immersed

$$\begin{aligned}\pi R^2 H &= \pi r^2 h \\ \pi \times 10 \times 10 \times h &= \pi \times 5 \times 5 \times 4 \\ h &= \frac{5 \times 5 \times 4}{10 \times 10} \\ &= 1\end{aligned}$$



The raise of the water in the glass = 1 cm

4. The volumes of two cones of same base radius are 3600 cm^3 and 5040 cm^3 . Find the ratio of heights.

PTA-4, MAY-22

$$\text{Volume of cone} = \frac{1}{3} \pi r^2 h$$

$$\text{Volume of cone 1 : Volume of cone 2} = 3600 : 5040$$

$$\frac{1}{3} \pi r^2 \times h_1 : \frac{1}{3} \pi r^2 \times h_2 = 180 : 252$$

$$h_1 : h_2 = 45 : 63$$

$$h_1 : h_2 = 5 : 7$$

5. A solid sphere and a solid hemisphere have equal total surface area. Prove that the ratio of their volume is $3\sqrt{3} : 4$.

PTA-6

TSA of sphere = TSA of hemisphere

$$4\pi r_1^2 = 3\pi r_2^2 \Rightarrow \frac{r_1^2}{r_2^2} = \frac{3}{4} \Rightarrow \frac{r_1}{r_2} = \frac{\sqrt{3}}{2}$$

$$\frac{\text{volume of sphere}}{\text{volume of hemisphere}} = \frac{\frac{4}{3}\pi r_1^3}{\frac{2}{3}\pi r_2^3}$$

$$= 2 \left(\frac{r_1}{r_2} \right)^3$$

$$= 2 \left(\frac{\sqrt{3}}{2} \right)^3$$

$$= \frac{2 \times 3\sqrt{3}}{8}$$

$$= \frac{3\sqrt{3}}{4}$$

∴ Ratio of the volume $3\sqrt{3} : 4$

6. Find the number of coins, 1.5 cm in diameter and 2 mm thick, to be melted to form a right circular cylinder of height 10 cm and diameter 4.5 cm. PTA-1

$$\begin{aligned} \text{Number of coins} &= \frac{\text{volume of cylinder } (\pi r^2 h)}{\text{volume of a coin } (\pi r^2 h)} \\ &= \frac{\pi \times 4.5 \times 4.5 \times 10 \times 10 \times 2 \times 10 \times 2 \times 10}{2 \times 10 \times 2 \times 10 \times \pi \times 1.5 \times 1.5 \times 2} \end{aligned}$$

Number of coins to be melted = **450 coins**

5 mark Questions

1. A container open at the top is in the form of a frustum of a cone of height 16 cm with radii of its lower and upper ends are 8 cm and 20 cm respectively. Find the cost of milk which can completely fill a container at the rate of ₹ 40 per litre. MAY-22

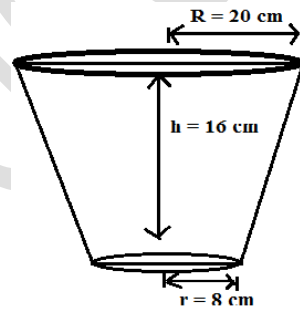
$$\begin{aligned} \text{Volume of frustum} &= \frac{1}{3} \pi h (R^2 + r^2 + Rr) \\ &= \frac{1}{3} \times \frac{22}{7} \times 16 (20^2 + 8^2 + (20 \times 8)) \\ &= \frac{1}{3} \times \frac{22}{7} \times 16 \times 624 \\ &= \frac{73216}{7} \\ &= 10459.4 \text{ cm}^3 \end{aligned}$$

Volume of frustum = 10.4594 litres

Required cost = 10.4594 × 40

$$= ₹ 418.376$$

Cost of the milk which can completely fill the container \cong ₹ **418.38**



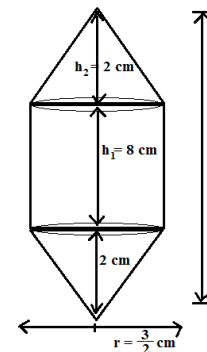
$$\therefore 1000 \text{ cm}^3 = 1 \text{ litre}$$

2. Nathan, an engineering student was asked to make a model shaped like a cylinder with two cones attached at its two ends. The diameter of the model is 3 cm and its length is 12 cm. If each cone has a height of 2 cm, find the volume of the model that Nathan made. MAY-22

Volume of the model = Volume of cylinder + Volume of cone × 2

$$\begin{aligned} &= \pi r^2 h_1 + \frac{1}{3} \pi r^2 h_2 \times 2 \\ &= \pi r^2 \left[h_1 + \frac{2}{3} h_2 \right] \\ &= \frac{22}{7} \times \frac{3}{2} \times \frac{3}{2} \times \left[8 + \frac{2}{3} (2) \right] \\ &= \frac{22}{7} \times \frac{3}{2} \times \frac{3}{2} \times \frac{28}{3} \end{aligned}$$

Volume of the model = **66 cm³**



3. A metallic sheet in the form of a sector of a circle of radius 21 cm has central angle of 216° . The sector is made into a cone by bringing the bounding radii together. Find the volume of the cone formed.

PTA-2

$$\text{Arc length } L = \frac{2\pi R}{360} \times 216$$

$$L = \frac{2\pi \times 21 \times 3}{5}$$

Circum of base of the cone = Arc length

$$\text{i.e, } 2\pi r = \frac{2\pi \times 21 \times 3}{5}$$

$$= \frac{63}{5}$$

$$r = 12.6\text{ cm}$$

$$h = \sqrt{l^2 - r^2}$$

$$= \sqrt{21^2 - 12.6^2}$$

$$= \sqrt{441 - 158.76}$$

$$= \sqrt{282.24}$$

$$h = 16.8\text{ cm}$$

$$\text{Volume of cone} = \frac{1}{3}\pi r^2 h$$

$$= \frac{1}{3} \times \frac{22}{7} \times 12.6 \times 12.6 \times 16.8$$

$$= 2794.176\text{ cm}^3$$

$$\text{Volume of the cone formed} = 2794.176\text{ cm}^3$$

